

# Package: BSPBSS (via r-universe)

September 10, 2024

**Title** Bayesian Spatial Blind Source Separation

**Version** 1.0.5

**Description** Gibbs sampling for Bayesian spatial blind source separation (BSP-BSS). BSP-BSS is designed for spatially dependent signals in high dimensional and large-scale data, such as neuroimaging. The method assumes the expectation of the observed images as a linear mixture of multiple sparse and piece-wise smooth latent source signals, and constructs a Bayesian nonparametric prior by thresholding Gaussian processes. Details can be found in our paper: Wu et al. (2022+) ``Bayesian Spatial Blind Source Separation via the Thresholded Gaussian Process" <[doi:10.1080/01621459.2022.2123336](https://doi.org/10.1080/01621459.2022.2123336)>.

**Depends** R (>= 3.4.0), movMF

**License** GPL (>= 3)

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 7.2.1

**LinkingTo** Rcpp, RcppArmadillo

**Imports** rstiefel, Rcpp, ica, glmnet, gplots, BayesGPfit, svd, neurobase, oro.nifti, gridExtra, ggplot2, gtools

**SystemRequirements** GNU make

**Suggests** knitr, rmarkdown

**VignetteBuilder** knitr

**Repository** <https://benwu233.r-universe.dev>

**RemoteUrl** <https://github.com/benwu233/bspbss>

**RemoteRef** HEAD

**RemoteSha** da762898b905718cdfd5657e597b638c3a57448d

## Contents

init_bspbss . . . . .	2
levelplot2D . . . . .	3
mcmc_bspbss . . . . .	4
output_nii . . . . .	5
pre_nii . . . . .	6
sim_2Dimage . . . . .	6
sum_mcmc_bspbss . . . . .	7

<b>Index</b>	<b>9</b>
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init_bspbss	<i>Initial values</i>
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## Description

Generate initial values, set up priors and perform kernel decomposition for the MCMC algorithm.

## Usage

```
init_bspbss(
  X,
  coords,
  rescale = TRUE,
  center = FALSE,
  q = 2,
  dens = 0.5,
  ker_par = c(0.05, 20),
  num_eigen = 500,
  noise = 0
)
```

## Arguments

X	Data matrix with n rows (sample) and p columns (voxel).
coords	Coordinate matrix with p rows (voxel) and d columns (dimension).
rescale	If TRUE, rows of X are rescaled to have unit variance.
center	If TRUE, rows of X are mean-centered.
q	Number of latent sources.
dens	The initial density level (between 0 and 1) of the latent sources.
ker_par	2-dimensional vector (a,b) with a>0, b>0, specifying the parameters in the modified exponential squared kernel.
num_eigen	Number of eigen functions.
noise	Gaussian noise added to the initial latent sources, with mean 0 and standard deviation being noise * sd(S0), where sd(S0) is the standard deviation of the initial latent sources.

**Value**

List containing initial values, priors and eigen functions/eigen values of the kernel of the Gaussian process.

**Examples**

```
sim = sim_2Dimage(length = 30, sigma = 5e-4, n = 30, smooth = 6)
ini = init_bspbss(sim$X, sim$coords, q = 3, ker_par = c(0.1,50), num_eigen = 50)
```

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levelplot2D	<i>levelplot for 2D images.</i>
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**Description**

The function plots 2D images for a data matrix.

**Usage**

```
levelplot2D(
  S,
  coords,
  lim = c(min(S), max(S)),
  xlim = c(0, max(coords[, 1])),
  ylim = c(0, max(coords[, 2])),
  color = bluered(100),
  layout = c(1, nrow(S)),
  file = NULL
)
```

**Arguments**

S	Data matrix with q rows (sample) and p columns (pixel).
coords	Coordinates matrix with p rows (pixel) and 2 columns (dimension), specifying the coordinates of the data points.
lim	2-dimensional numeric vector, specifying the limits for the data.
xlim	2-dimensional numeric vector, specifying the lower and upper limits of x.
ylim	2-dimensional numeric vector, specifying the lower and upper limits of y.
color	Colorbar.
layout	2-dimensional numeric vector, specifying the number of rows and number of columns for the layout of components.
file	Name of the file to be saved.

**Value**

No return value.

**Examples**

```
sim = sim_2Dimage(length = 30, sigma = 5e-4, n = 30, smooth = 6)
levelplot2D(sim$S,lim = c(-0.04,0.04), sim$coords)
```

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mcmc\_bspbss

*MCMC algorithm for Bayesian spatial blind source separation with the thresholded Gaussian Process prior.*

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**Description**

Performan MCMC algorithm to draw samples from a Bayesian spatial blind source separation model.

**Usage**

```
mcmc_bspbss(
  X,
  init,
  prior,
  kernel,
  n.iter,
  n.burn_in,
  thin = 1,
  show_step,
  ep = 0.01,
  lr = 0.01,
  decay = 0.01,
  num_leapfrog = 5,
  subsample_n = 0.5,
  subsample_p = 0.5
)
```

**Arguments**

X	Data matrix with n rows (sample) and p columns (voxel).
init	List of initial values, see <code>init_bspbss</code> .
prior	List of priors, see <code>init_bspbss</code> .
kernel	List including eigenvalues and eigenfunctions of the kernel, see <code>init_bspbss</code> .
n.iter	Total iterations in MCMC.
n.burn_in	Number of burn-in.
thin	Thining interval.
show_step	Frequency for printing the current number of iterations.
ep	Approximation parameter.

lr	Per-batch learning rate in SGHMC.
decay	Decay parameter in SGHMC.
num_leapfrog	Number of leapfrog steps in SGHMC.
subsample_n	Mini-batch size of samples.
subsample_p	Mini-batch size of voxels.

**Value**

List containing MCMC samples of: A, b, sigma, and zeta.

**Examples**

```
sim = sim_2Dimage(length = 30,
                  sigma = 5e-4,
                  n = 30,
                  smooth = 6)
ini = init_bspbss(sim$X, sim$coords,
                 q = 3,
                 ker_par = c(0.1,50),
                 num_eigen = 50)
res = mcmc_bspbss(ini$X, ini$init,
                 ini$prior, ini$kernel,
                 n.iter=200, n.burn_in=100,
                 thin=10, show_step=50)
```

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output_nii	<i>Write a NIfTI file.</i>
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**Description**

This function saves a data matrix into a NIfTI file.

**Usage**

```
output_nii(X, nii, xgrid, file = NULL, std = TRUE, thres = 0)
```

**Arguments**

X	Data matrix with n rows (sample) and p columns (pixel).
nii	a reference NIfTI-class object, representing a image with p voxels.
xgrid	Cordinate matrix with p rows (voxel) and d columns (dimension).
file	The name of the file to be saved.
std	If TRUE, standarize each row of X.
thres	Quantile to threshold each row of X.

**Value**

NIfTI-class object.

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pre_nii	<i>Transforms NIfTI to matrix</i>
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**Description**

This function transforms a NIfTI-class object into a matrix.

**Usage**

```
pre_nii(nii, mask)
```

**Arguments**

nii	4D NIfTI-class object with dimensions x,y,z and t. Can be read from NIfTI file with readNIfTI function from the package oro.nifti.
mask	Mask variable, also in NIfTI format.

**Value**

List containing the data matrix with t rows and x\*y\*z columns (voxels), and the coordinates of the voxels.

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sim_2Dimage	<i>Simulate image data using ICA</i>
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**Description**

The function simulates image data using a probabilistic ICA model whose latent components have specific spatial patterns.

**Usage**

```
sim_2Dimage(length = 20, n = 50, sigma = 0.002, smooth = 6)
```

**Arguments**

length	The length of the image.
n	sample size.
sigma	variance of the noise.
smooth	smoothness of the latent components.

## Details

The observations are generated using probabilistic ICA:

$$X_i(v) = \sum_{j=1}^q A_{i,j} S_j(v) + \epsilon_i(v),$$

where  $S_j, j = 1, \dots, q$  are the latent components,  $A_{i,j}$  is the mixing coefficient and  $\epsilon_i$  is the noise term. Specifically, the number of components in this function is  $q = 3$ , with each of them being a specific geometric shape. The mixing coefficient matrix is generated with a von Mises-Fisher distribution with the concentration parameter being zero, which means it is uniformly distributed on the sphere.  $\epsilon_i$  is a i.i.d. Gaussian noise term with 0 mean and user-specified variance.

## Value

List that contains the following terms:

**X** Data matrix with n rows (sample) and p columns (pixel).

**coords** Coordinate matrix with p rows (pixel) and d columns (dimension)

**S** Latent components.

**A** Mixing coefficient matrix.

**snr** Signal-to-noise ratio.

## Examples

```
sim = sim_2Dimage(length = 30, sigma = 5e-4, n = 30, smooth = 6)
```

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sum\_mcmc\_bspbss

*Summarization of the MCMC result.*

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## Description

The function summarizes the MCMC results obtained from `mcmc_bspbss`.

## Usage

```
sum_mcmc_bspbss(res, X, kernel, start = 1, end = 100, select_prob = 0.8)
```

## Arguments

<code>res</code>	List including MCMC samples, which can be obtained from function <code>mcmc_bspbss</code>
<code>X</code>	Original data matrix.
<code>kernel</code>	List including eigenvalues and eigenfunctions of the kernel, see <code>init_bspbss</code> .
<code>start</code>	Start point of the iterations being summarized.
<code>end</code>	End point of the iterations being summarized.
<code>select_prob</code>	Lower bound of the posterior inclusion probability required when summarizing the samples of latent sources.

**Value**

List that contains the following terms:

**S** Estimated latent sources.

**pip** Voxel-wise posterior inclusion probability for the latent sources.

**A** Estimated mixing coefficient matrix.

**zeta** Estimated zeta.

**sigma** Estimated sigma.

**logLik** Trace of log-likelihood.

**Slist** MCMC samples of S.

**Examples**

```
sim = sim_2Dimage(length = 30, sigma = 5e-4, n = 30, smooth = 6)
ini = init_bspbss(sim$X, sim$coords, q = 3, ker_par = c(0.1,50), num_eigen = 50)
res = mcmc_bspbss(ini$X, ini$init, ini$prior, ini$kernel, n.iter=200, n.burn_in=100, thin=10, show_step=50)
res_sum = sum_mcmc_bspbss(res, ini$X, ini$kernel, start = 11, end = 20, select_p = 0.5)
```



# Index

`init_bspbss`, 2

`levelplot2D`, 3

`mcmc_bspbss`, 4

`output_nii`, 5

`pre_nii`, 6

`sim_2Dimage`, 6

`sum_mcmc_bspbss`, 7